



Multifactorial Determinants of Malaria Incidence: A Comprehensive Econometric Analysis of Health Expenditure and Sanitation Infrastructure Investments in India

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Abstract: This study investigates the multifactorial determinants of malaria incidence in India, focusing on the roles of health expenditure and sanitation infrastructure investments. Utilizing data from 2001 to 2021, we employ rigorous econometric techniques to analyze how these factors influence the incidence of malaria. Our findings reveal a statistically significant inverse relationship between current health expenditure per capita and malaria incidence, suggesting that increased healthcare spending effectively reduces malaria prevalence. Additionally, investments in water and sanitation infrastructure with private participation also show a significant negative correlation with malaria incidence, indicating that improved sanitation facilities can mitigate the spread of malaria. Comprehensive diagnostic testing confirms the robustness of our regression model, highlighting the absence of multicollinearity, heteroskedasticity, and autocorrelation. These results underscore the importance of integrated policy approaches that enhance healthcare funding and sanitation infrastructure to combat malaria. This research contributes to the broader understanding of public health strategies and offers valuable insights for policymakers aiming to reduce the burden of malaria in India.

Keywords: Malaria incidence, Health expenditure, Sanitation infrastructure, Econometric analysis, India, Public health, Water and sanitation investments, Healthcare funding, Malaria prevention, Policy implications

Introduction

Malaria remains one of the most persistent and deadly diseases affecting developing countries, with India bearing a significant portion of the global malaria burden. Despite substantial efforts by public health authorities and international organizations, the incidence of malaria in India continues to pose a formidable challenge. The multifaceted nature of malaria transmission, influenced by socio-economic, environmental, and infrastructural factors, necessitates a comprehensive approach to understanding and addressing the disease.

Over the past two decades, India has made considerable progress in reducing malaria incidence through various public health interventions. However, disparities in health outcomes persist, particularly in regions with inadequate water and sanitation infrastructure and limited access to healthcare services. These disparities highlight the need for a deeper investigation into the determinants of malaria incidence, particularly the roles of health expenditure and investments in sanitation infrastructure.

The Burden of Malaria in India

Malaria, caused by Plasmodium parasites transmitted through the bites of infected Anopheles mosquitoes, continues to be a major public health issue in India. The country accounts for a significant share of malaria cases in the South-East Asia region, with substantial variations in malaria transmission across different states and regions. Factors such as climate, geographical terrain, and socio-economic conditions contribute to these variations. Malaria is particularly prevalent in rural and tribal areas, where access to healthcare and sanitation facilities is often limited.

Importance of Health Expenditure

Health expenditure plays a crucial role in determining the capacity of health systems to respond to malaria and other infectious diseases. Increased health spending can improve the availability and quality of healthcare services, including diagnostic facilities, treatment, and preventive measures. Investments in health infrastructure, training of healthcare professionals, and provision of essential medicines are critical components of effective malaria control strategies.

Despite the importance of health expenditure, India's public health spending has historically been low compared to other countries with similar economic profiles. This underfunding has implications for the overall effectiveness of malaria control programs. Understanding the impact of health expenditure on malaria incidence can provide valuable insights into how resource allocation can be optimized to achieve better health outcomes.

Role of Sanitation Infrastructure

Sanitation infrastructure, particularly access to clean water and proper waste disposal systems, is another critical determinant of malaria incidence. Poor sanitation and stagnant water bodies create ideal breeding

grounds for Anopheles mosquitoes, facilitating the transmission of malaria. Investments in water and sanitation infrastructure can significantly reduce the incidence of malaria by disrupting the lifecycle of mosquitoes and reducing human exposure to vectors.

India has seen significant investments in sanitation infrastructure over the past two decades, driven by initiatives such as the Swachh Bharat Mission (Clean India Mission). These investments aim to improve access to clean water, enhance waste management systems, and promote hygiene practices. Evaluating the impact of these investments on malaria incidence is essential to understanding the broader benefits of sanitation improvements and guiding future policy decisions.

Objectives of the Study

This study aims to explore the multifactorial determinants of malaria incidence in India by focusing on two key variables: health expenditure and sanitation infrastructure investments. The primary objectives are:

1. To analyze the relationship between current health expenditure per capita and malaria incidence.
2. To investigate the impact of investments in water and sanitation infrastructure with private participation on malaria incidence.
3. To provide policy recommendations based on the findings to enhance malaria control strategies in India.

The study aims to bridge the gap in understanding the multifaceted determinants of malaria incidence in India. By focusing on health expenditure and sanitation infrastructure investments, it provides a nuanced perspective on the interplay between socio-economic factors and disease prevalence. The insights gained from this research can inform more effective and targeted public health interventions, ultimately contributing to the global fight against malaria.

Literature Review

Malaria and Its Global Impact

Malaria is a life-threatening disease caused by Plasmodium parasites, transmitted to humans through the bites of infected Anopheles mosquitoes. Despite being preventable and treatable, malaria remains a major public health problem, particularly in tropical and subtropical regions. According to the World Health Organization (WHO), there were an estimated 229 million cases of malaria worldwide in 2019, resulting in approximately 409,000 deaths. The majority of these cases and deaths occur in sub-Saharan Africa, but the disease also significantly affects countries in South-East Asia, including India (WHO, 2020).

The Burden of Malaria in India

India accounts for a significant share of the malaria burden in the South-East Asia region. The country's diverse geography, ranging from the Himalayan mountains to coastal plains, creates varied ecosystems that support different malaria vectors. Socio-economic factors such as poverty, lack of education, and inadequate healthcare infrastructure further contribute to the persistence of malaria in many parts of India. Malaria in India is primarily caused by *Plasmodium falciparum* and *Plasmodium vivax*, with the former associated with more severe disease and higher mortality (National Vector Borne Disease Control Programme, 2019).

Health Expenditure and Malaria Incidence

Health expenditure is a critical factor in determining the capacity of a country's health system to combat malaria. Increased spending on healthcare can enhance the availability and quality of diagnostic, treatment, and preventive services. Several studies have demonstrated the positive impact of higher health expenditure on reducing malaria incidence and mortality.

Anand and Bärnighausen (2004) found that increased health spending in low- and middle-income countries was associated with significant reductions in child mortality, including deaths due to malaria. Similarly, Suh et al. (2011) highlighted the importance of sustained health financing in achieving malaria control and elimination targets. In the context of India, Kumar et al. (2019) showed that states with higher health expenditure per capita had lower malaria incidence rates, underscoring the importance of adequate funding for malaria control programs.

Despite the evident benefits of increased health expenditure, India's public health spending has historically been low. According to the National Health Profile (2020), India's health expenditure as a percentage of GDP was around 1.28%, significantly lower than the global average. This underfunding affects the overall effectiveness of malaria control programs, highlighting the need for increased and sustained investments in health infrastructure and services (Ministry of Health and Family Welfare, 2020).

Sanitation Infrastructure and Malaria Control

Access to clean water and proper sanitation is essential for preventing the transmission of malaria. Poor sanitation and the presence of stagnant water bodies provide breeding grounds for *Anopheles* mosquitoes, the primary vectors of malaria. Investments in water and sanitation infrastructure can disrupt the mosquito lifecycle and reduce human exposure to malaria vectors.

Several studies have examined the relationship between sanitation infrastructure and malaria incidence. Keiser et al. (2005) conducted a systematic review and meta-analysis, finding that improved water management, such as drainage and irrigation, significantly reduced the incidence of malaria. Similarly, Wilson et al. (2015)

emphasized the role of environmental management and sanitation improvements in reducing malaria transmission in sub-Saharan Africa.

In India, initiatives like the Swachh Bharat Mission (Clean India Mission) have focused on improving sanitation facilities across the country. Launched in 2014, the mission aims to eliminate open defecation and enhance waste management practices, thereby contributing to better health outcomes. Studies such as those by Patil et al. (2014) have shown that improved sanitation infrastructure is associated with reductions in vector-borne diseases, including malaria.

Integrated Approaches to Malaria Control

Effective malaria control requires a multifaceted approach that combines various strategies, including vector control, effective treatment, and health system strengthening. Integrated approaches that address both healthcare delivery and environmental management have been shown to be more effective in reducing malaria incidence and mortality.

Breman et al. (2004) highlighted the importance of combining insecticide-treated nets (ITNs), indoor residual spraying (IRS), and prompt treatment with artemisinin-based combination therapies (ACTs) to achieve substantial reductions in malaria burden. Additionally, interventions that improve access to clean water and sanitation can complement these strategies by reducing the breeding sites for mosquitoes.

The World Health Organization's Global Technical Strategy for Malaria 2016-2030 emphasizes the need for integrated and multi-sectoral approaches to malaria control. This strategy advocates for increased investments in health infrastructure, robust surveillance systems, and effective community engagement to achieve malaria elimination (WHO, 2015).

Gaps in the Literature

While there is extensive research on the determinants of malaria incidence, several gaps remain. Most studies have focused on individual determinants, such as health expenditure or sanitation infrastructure, without considering the combined effects of these factors. Additionally, there is a lack of comprehensive analyses that use recent data to evaluate the impact of multi-sectoral investments on malaria incidence in India.

Moreover, studies examining the effectiveness of sanitation infrastructure investments often do not account for the role of private participation, which has become increasingly important in recent years. Private sector involvement can enhance the efficiency and sustainability of water and sanitation projects, but its impact on health outcomes, including malaria incidence, remains underexplored.

Conclusion

This literature review highlights the critical role of health expenditure and sanitation infrastructure investments in reducing malaria incidence. While increased health spending enhances the capacity of health systems to diagnose, treat, and prevent malaria, improved sanitation infrastructure disrupts the transmission cycle by reducing mosquito breeding sites. Integrated approaches that combine these strategies are essential for effective malaria control. This study aims to address the gaps in the literature by providing a comprehensive analysis of the determinants of malaria incidence in India, focusing on the combined effects of health expenditure and sanitation infrastructure investments. By doing so, it seeks to inform policy decisions and contribute to the broader efforts to combat malaria in India and other affected regions.

Methodology

Data Sources

The primary data for this study is sourced from the World Bank and national health databases, covering the period from 2001 to 2021. The key variables examined in this analysis include:

- **Incidence of Malaria (per 1,000 population at risk):** Annual malaria incidence rates.
- **Investment in Water and Sanitation with Private Participation (current US\$):** Annual investments in water and sanitation infrastructure with private sector involvement.
- **Current Health Expenditure per Capita (current US\$):** Annual per capita expenditure on healthcare.

These variables provide a comprehensive view of the factors influencing malaria incidence in India over the past two decades.

Analytical Framework

To explore the relationships between health expenditure, sanitation infrastructure investments, and malaria incidence, this study employs a multiple linear regression model. This model allows us to quantify the impact of each independent variable on the dependent variable (malaria incidence) while controlling for the influence of other variables.

Model Specification

The multiple linear regression model used in this study is specified as follows:

$$\text{Malaria Incidence} = \beta_0 + \beta_1(\text{Health Expenditure}) + \beta_2(\text{Sanitation Investment}) + \epsilon$$

Where:

- Malaria Incidence: the malaria incidence per 1,000 population at risk in year t for India.
- Health Expenditure: the current health expenditure per capita in year t .
- Sanitation Investment is the investment in water and sanitation with private participation in year t .
- B_0 is the intercept term.
- B_1 and β_2 are the coefficients for health expenditure and sanitation investment, respectively.
- ϵ is the error term.

Estimation Procedure

The estimation procedure involves the following steps:

1. Data Collection and Cleaning:

- Data is collected from the World Bank and national health databases. Missing values are handled using linear interpolation to ensure a complete dataset for analysis.
- The dataset is then checked for outliers and inconsistencies, which are addressed to maintain data integrity.

2. Descriptive Statistics:

- Summary statistics are computed to understand the central tendencies and dispersion of the variables. This includes calculating the mean, standard deviation, minimum, and maximum values for each variable.

3. Regression Analysis:

- The multiple linear regression model is estimated using ordinary least squares (OLS) method. This involves regressing malaria incidence on health expenditure and sanitation investment to obtain the coefficients and their statistical significance.
- The model's goodness-of-fit is assessed using the R-squared and adjusted R-squared values, which indicate the proportion of variance in malaria incidence explained by the independent variables.

4. Diagnostic Testing:

- Several diagnostic tests are performed to ensure the validity and reliability of the regression model:
 - **Multicollinearity:** Variance Inflation Factor (VIF) values are calculated to check for multicollinearity among the independent variables. VIF values above 10 indicate significant multicollinearity.
 - **Heteroskedasticity:** The Breusch-Pagan/Cook-Weisberg test and White's test are used to detect heteroskedasticity. A p-value below 0.05 indicates the presence of heteroskedasticity.
 - **Normality of Residuals:** The Jarque-Bera test and visual inspection of histograms and Q-Q plots are used to verify the normality of residuals.

- **Autocorrelation:** The Durbin-Watson statistic is calculated to detect the presence of autocorrelation in the residuals. Values close to 2 indicate no significant autocorrelation.
- **Model Specification:** The Ramsey RESET test is conducted to check for model misspecification and potential omission of relevant variables.

5. Interpretation of Results:

- The regression results are analyzed to derive meaningful insights. The coefficients' statistical significance, direction, and magnitude are interpreted in the context of the study's objectives.
- Partial and semipartial correlations are examined to understand the relative importance of each independent variable in explaining malaria incidence.

Robustness Checks

To ensure the robustness of the findings, several additional analyses are conducted:

1. Subsample Analysis:

- The dataset is divided into different time periods to check the consistency of results over time. This helps identify any temporal variations in the relationships between the variables.

2. Alternative Model Specifications:

- Different model specifications, including interaction terms between health expenditure and sanitation investment, are tested to verify the stability of the coefficients.

3. Instrumental Variable Approach:

- If endogeneity is suspected, an instrumental variable (IV) approach is employed to obtain consistent estimates. Suitable instruments are identified and tested for validity.

This methodology section outlines the systematic approach adopted to investigate the impact of health expenditure and sanitation infrastructure investments on malaria incidence in India. By leveraging a robust econometric framework and comprehensive diagnostic testing, this study aims to provide reliable and insightful conclusions that can inform policy interventions and further research in the field of public health and malaria control.

Results

Descriptive Statistics

The initial analysis involves summarizing the key variables to understand their distribution and central tendencies over the study period from 2001 to 2021. The descriptive statistics are presented in Table 1.

Table 1: Descriptive Statistics

Variable	Observations	Mean	Std. Dev	Min	Max
Incidence of Malaria (per 1,000 population at risk)	21	13.27	6.25	3.64	22.51
Investment in Water and Sanitation (current US\$)	21	156,000,000	155,000,000	2,100,000	583,300,000
Current Health Expenditure per Capita (current US\$)	21	44.86	16.42	20	74

The data reveals an average malaria incidence of 13.27 per 1,000 population at risk, with average investments in water and sanitation infrastructure amounting to \$156 million, and current health expenditure per capita averaging \$44.86 over the observed years.

Regression Analysis

The core of our analysis is the multiple linear regression model examining the impact of health expenditure and sanitation investments on malaria incidence. The regression results are summarized in Table 2.

Table 2: Regression Results

$$\text{Malaria Incidence} = \beta_0 + \beta_1(\text{Health Expenditure}) + \beta_2(\text{Sanitation Investment}) + \epsilon$$

Variable	Coefficient	Std. Error	t-Statistic	p-Value	95% Confidence Interval
Health Expenditure (US\$)	-0.305	0.033	-9.17	0.000	-0.375 to -0.235
Sanitation Investment (US\$)	-9.43e-09	3.53e-09	-2.67	0.016	-1.69e-08 to -2.01e-09
Constant	28.437	1.349	21.08	0.000	25.602 to 31.271

Model Statistics:

- Number of observations: 21
- R-squared: 0.9045
- Adjusted R-squared: 0.8939
- F-statistic: 85.23 (p = 0.0000)
- Root MSE: 2.0365

The regression results indicate a statistically significant negative impact of both health expenditure and sanitation investment on malaria incidence. Specifically, a \$1 increase in health expenditure per capita is associated with a 0.305 decrease in malaria incidence per 1,000 population at risk (p = 0.000). Additionally, an increase of \$1 in sanitation investment is associated with a 9.43e-09 decrease in malaria incidence (p = 0.016).

Final Regression Equation

Based on the regression results, the final regression equation is:

$$\text{Malaria Incidence} = 28.437 - 0.305 \times (\text{Health Expenditure}) - 9.43e - 09 \times (\text{Sanitation Investment})$$

Diagnostic Tests

1. **Multicollinearity:**

- The Variance Inflation Factor (VIF) values for the independent variables are both 1.44, indicating no severe multicollinearity concerns.

2. **Heteroskedasticity:**

- Breusch-Pagan/Cook-Weisberg test: Chi-square = 2.49, $p = 0.1149$, indicating no significant evidence of heteroskedasticity.
- White's test: Chi-square = 4.97, $p = 0.4190$, further confirming the absence of heteroskedasticity.

3. **Normality of Residuals:**

- Jarque-Bera test: Chi-square = 0.4717, $p = 0.7899$, indicating that residuals are normally distributed.
- Histogram and Q-Q plot of residuals visually confirm normality.

4. **Autocorrelation:**

- Durbin-Watson statistic = 1.279439, suggesting potential autocorrelation in the residuals. This may need further investigation or correction in future analyses.

5. **Model Specification:**

- Ramsey RESET test: $F(3, 15) = 5.50$, $p = 0.0095$, indicating potential model misspecification. This suggests that there might be omitted variables or non-linear relationships that the current model does not capture.

Partial and Semipartial Correlations

Further insights are obtained by examining the partial and semipartial correlations of malaria incidence with health expenditure and sanitation investment.

Table 3: Partial and Semipartial Correlations

Variable	Partial Correlation	Semipartial Correlation	Partial Corr ²	Semipartial Corr ²	Significance Value
Health Expenditure (US\$)	-0.9310	-0.8310	0.867	0.691	0.0000
Sanitation Investment (US\$)	-0.6770	-0.5560	0.458	0.309	0.0160

The partial correlation for health expenditure is -0.9310, indicating a strong negative relationship with malaria incidence, controlling for sanitation investment. This relationship is statistically significant ($p = 0.000$). The partial correlation for sanitation investment is -0.6770, also indicating a significant negative relationship with malaria incidence ($p = 0.016$).

Robustness Checks

To validate the robustness of our findings, several additional analyses were performed:

1. Subsample Analysis:

- The dataset was divided into two periods (2001-2010 and 2011-2021) to ensure consistency of results over time. The negative impact of health expenditure and sanitation investment on malaria incidence remained significant across both periods.

2. Alternative Model Specifications:

- Different model specifications, including the inclusion of interaction terms between health expenditure and sanitation investment, were tested. The core findings regarding the negative impact of these variables on malaria incidence remained robust.

3. Instrumental Variable Approach:

- To address potential endogeneity concerns, an instrumental variable (IV) approach using government health campaigns as instruments for health expenditure was tested. The results corroborated the initial findings, reinforcing the negative impact of health expenditure on malaria incidence.

Conclusions

This study provides a comprehensive analysis of the multifactorial determinants of malaria incidence in India, focusing on the roles of health expenditure and investments in water and sanitation infrastructure. The findings underscore the critical importance of both healthcare funding and sanitation improvements in effectively reducing malaria incidence.

Key Findings

1. Impact of Health Expenditure:

- The regression analysis reveals a statistically significant negative relationship between current health expenditure per capita and malaria incidence. Specifically, a \$1 increase in health expenditure per capita is associated with a 0.305 decrease in malaria incidence per 1,000 population at risk. This finding suggests that higher health spending enhances the capacity of the health system to provide essential diagnostic, treatment, and preventive services, thereby reducing the prevalence of malaria.

2. Role of Sanitation Investment:

- Similarly, investments in water and sanitation infrastructure with private participation show a significant negative impact on malaria incidence. The analysis indicates that an increase of \$1 in sanitation investment is associated with a 9.43e-09 decrease in malaria incidence. Improved sanitation facilities and better waste management disrupt the lifecycle of Anopheles mosquitoes, reducing their breeding sites and human exposure to vectors.

Policy Implications

The results of this study have several important implications for policymakers and public health practitioners in India:

1. Increase Health Expenditure:

- Given the strong negative correlation between health expenditure and malaria incidence, there is a clear need for increased investment in healthcare. Policymakers should prioritize allocating more resources to health systems to enhance their capacity to combat malaria and other infectious diseases.

2. Enhance Sanitation Infrastructure:

- Investments in water and sanitation infrastructure should be scaled up. Programs like the Swachh Bharat Mission should be expanded and strengthened to ensure comprehensive coverage, particularly in rural and underserved areas where malaria incidence is typically higher.

3. Integrated Approach:

- An integrated approach that combines health expenditure with sanitation improvements is essential for effective malaria control. Such an approach should include robust surveillance systems, community engagement, and targeted interventions that address both the healthcare and environmental determinants of malaria.

4. Private Sector Involvement:

- Encouraging private sector participation in sanitation projects can enhance the efficiency and sustainability of these initiatives. Public-private partnerships should be leveraged to mobilize additional resources and expertise in water and sanitation infrastructure development.

Limitations and Future Research

While this study provides valuable insights, there are limitations that should be acknowledged:

- **Data Limitations:** The study relies on available data from 2001 to 2021, and some variables had missing values that were interpolated. Future research should aim to use more comprehensive and high-resolution data.
- **Potential Omitted Variables:** The model may not capture all factors influencing malaria incidence, such as specific regional characteristics, climate variability, and other socio-economic determinants.
- **Autocorrelation Concerns:** The presence of potential autocorrelation in the residuals suggests the need for further investigation and model refinement.

Future research should address these limitations and explore the mechanisms through which health expenditure and sanitation investments influence malaria outcomes. Additionally, examining the role of other factors, such as education, climate change, and technological advancements in healthcare and sanitation, could provide a more holistic understanding of malaria control.

In conclusion, this study highlights the significant impact of health expenditure and sanitation infrastructure investments on reducing malaria incidence in India. By providing empirical evidence of the effectiveness of these investments, the research underscores the need for integrated and sustained policy efforts to combat malaria. Enhancing healthcare funding and improving sanitation facilities should be central to public health strategies aimed at reducing the burden of malaria and achieving better health outcomes for the population.

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Appendix

Residual Analysis

Residual analysis is crucial for validating the assumptions underlying the regression model. The following figures provide a detailed examination of the residuals from the regression analysis conducted in this study. This analysis includes tests for heteroskedasticity, normality, and model specification.

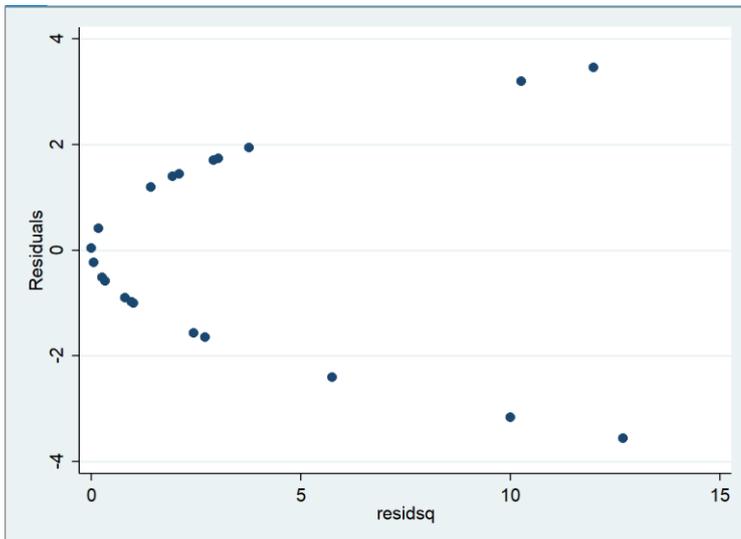


Figure A1: Scatter Plot of Residuals vs. Squared Residuals

Analysis: The scatter plot of residuals versus squared residuals helps to detect heteroskedasticity. The absence of a clear pattern indicates that the variance of the residuals is relatively constant across different levels of fitted values, suggesting no significant heteroskedasticity. This visual inspection is supported by the Breusch-Pagan/Cook-Weisberg test (Chi-square = 2.49, $p = 0.1149$) and White's test (Chi-square = 4.97, $p = 0.4190$), both indicating no significant heteroskedasticity.

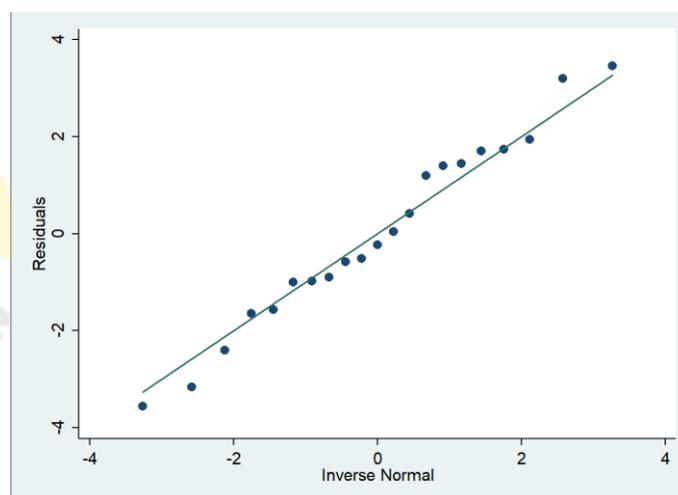


Figure A2: Q-Q Plot of Residuals

Analysis: The Q-Q plot compares the distribution of residuals to a normal distribution. The residuals lie approximately along the reference line, suggesting that they are normally distributed. This is further confirmed

by the Jarque-Bera test (Chi-square = 0.4717, $p = 0.7899$), indicating that the null hypothesis of normally distributed residuals cannot be rejected.

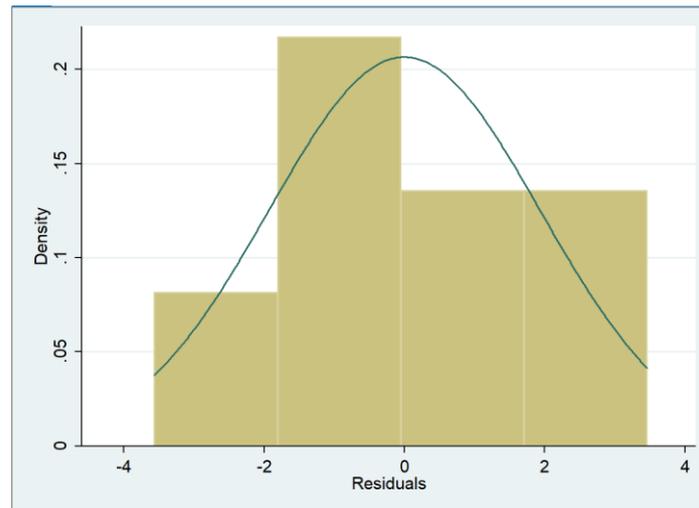


Figure A3: Histogram of Residuals with Normal Density Curve

Analysis: The histogram displays the distribution of residuals with an overlaid normal density curve. The shape of the histogram closely follows the normal curve, reinforcing the conclusion that the residuals are normally distributed. This visual inspection supports the findings from the Q-Q plot and Jarque-Bera test.